

MARKING SCHEME – SET II

SECTION – A

1.  $a^5b^5$ . (1 Mark)
2. Ans :  $\frac{34}{9}$  (1 Mark)
3. No (1mark)
4. Ans:  $\sqrt{a^2 + b^2}$  (1 Mark)
5. Ans: 7.2 cm (1 Mark)
6. Ans :  $A + 25 + B = 90$   
 $A + B = 65$  (1 Mark)

SECTION – B

7. Ans:  
 $11(7 \times 13 + 1)$  (1mark)  
Yes, It is expressed as a product of two factors (1mark)

8. Ans:

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}; \frac{3}{2k-1} = \frac{1}{k-1} \neq \frac{1}{2k+1}$$
$$k = 2 \text{ and } k \neq -\frac{1}{2} \Rightarrow k = 2$$

1

1

9. Ans:

Sol:

In A.P the first term = a and common difference = d.

Given that 9<sup>th</sup> term of an A.P. is 0.

Therefore  $t_9 = 0$

$$\Rightarrow a + 8d = 0 \Rightarrow a = -8d \text{ -----(1)}$$

1/2 mark

We have to prove that  $t_{29} = 2 t_{19}$ .

$$t_{19} = a + 18d = -8d + 18d = 10d \quad [ \text{ from (1) } ] \quad 1/2 \text{ mark}$$

$$t_{29} = a + 28d = -8d + 28d = 20d \quad [ \text{ from (1) } ] \quad 1/2 \text{ mark}$$

$$t_{29} = 2 \times 10d = 2 \times t_{19}$$

$$\therefore t_{29} = 2 \times t_{19} .$$

1/2 mark

10. Ans:

Let the ratio be k:1

$$3\left(\frac{4k+2}{k+1}\right) + 2\left(\frac{7k+1}{k+1}\right) = 10$$

(1mark)

$$26k - 10k = 10 - 8$$

$\left(\frac{1}{2}\right)$  mark)

Then the ratio is 1:8

$\left(\frac{1}{2}\right)$  mark)

11. Ans:

(i) Number of ways in which two dice can be thrown at the same time = 36

Multiple of 3 as the sum (1,3), (1,6), (2,3), (2,6), (3,1), (3,2), (3,3), (3,4), (3,5),  
(3,6), (4,3), (4,6), (5,3), (5,6), (6,1), (6,2), (6,3), (6,4), (6,5), (6,6)

$$p(\text{getting a multiple of 3 as sum}) = \frac{20}{36} = \frac{5}{9} \quad (1 \text{ mark})$$

(ii) 6 as the product (1,6), (2,3), (3,2), (6,1)

$$P(6 \text{ as the product}) = \frac{4}{36} = \frac{1}{9} \quad (1 \text{ mark})$$

12.

Ans: Let  $x$  be number of green balls

$$p(x) = \frac{2}{3} \quad (\frac{1}{2} \text{ mark})$$

$$\frac{x}{24} = \frac{2}{3}, x = 16 \quad (1 \text{ mark})$$

$$\text{So, number of blue balls} = 24 - 16 = 8. \quad (\frac{1}{2} \text{ mark})$$

### SECTION -C

13.

Let us suppose that  $\sqrt{6} + \sqrt{2}$  is rational

Then  $\sqrt{6} + \sqrt{2} = \frac{a}{b}$  where  $a$  and  $b$  are integers  $\frac{1}{2}$

$$8 + 2\sqrt{12} = \frac{a^2}{b^2}$$

$$8 + 4\sqrt{3} = \frac{a^2}{b^2} \quad \frac{1}{2}$$

$$\sqrt{3} = \frac{\frac{a^2}{b^2} - 8}{4} \quad \frac{1}{2}$$

$$\therefore a, b \text{ and } 6 \text{ are integers then } \frac{\frac{a^2}{b^2} - 8}{4} \text{ is rational} \quad \frac{1}{2}$$

$$\Rightarrow \sqrt{3} = \text{rational}$$

But we know that  $\sqrt{3}$  is irrational  $\frac{1}{2}$

$\Rightarrow$  irrational = rational which is a contradiction  $\frac{1}{2}$

Hence  $\sqrt{6} + \sqrt{2}$  is irrational.

14.

$$\begin{aligned}
 x = 2 \pm \sqrt{3} & \text{ are the zeroes of } p(x), \text{ so} \\
 x - (2 \pm \sqrt{3}) & \text{ are the factors of } p(x). \\
 \text{Now, } \left\{ x - (2 + \sqrt{3}) \right\} \left\{ x - (2 - \sqrt{3}) \right\} \\
 = \left\{ (x - 2) - \sqrt{3} \right\} \left\{ (x - 2) + \sqrt{3} \right\} \\
 = (x - 2)^2 - (\sqrt{3})^2 \\
 = x^2 - 4x + 1 & \quad \text{1 mark}
 \end{aligned}$$

Dividing  $p(x)$  by  $x^2 - 4x + 1$

$$\begin{array}{r}
 x^2 - 2x - 35 \\
 x^2 - 4x + 1 \overline{) x^4 - 6x^3 - 26x^2 + 138x - 35} \\
 \underline{x^4 - 4x^3 + x^2} \phantom{- 35} \\
 -2x^3 - 27x^2 + 138x \phantom{- 35} \\
 \underline{-2x^3 + 8x^2 - 2x} \phantom{- 35} \\
 -35x^2 + 140x - 35 \\
 \underline{-35x^2 + 140x - 35} \\
 0
 \end{array}$$

1 mark

$$x^2 - 2x - 35 = (x - 7)(x + 5)$$

Zeros are 7, -5,  $2 \pm \sqrt{3}$

(1 mark)

15.

Ans: The line  $y = 4$

$(\frac{1}{2}$  marks)

The line  $2x + y = 6$ , points (0,6) and (3,0)

(1 marks)

The vertices are (0,0), (3,0), (1,4) and (0,4)

$(\frac{1}{2}$  marks)

Area =  $\frac{1}{2} \times 4(1 + 3) = 16$  square units

(1 mark)

16. Show that the points  $(-4, -1)$ ,  $(-2, -4)$ ,  $(4,0)$  and  $(2,3)$  are the vertices of a rectangle.

$$AB = \sqrt{13} \text{ units}$$

$(\frac{1}{2}$  marks)

$$BC = \sqrt{52} \text{ units}$$

$(\frac{1}{2}$  marks)

$$CD = \sqrt{13} \text{ units}$$

$(\frac{1}{2}$  marks)

$$DA = \sqrt{52} \text{ units}$$

$(\frac{1}{2}$  marks)

$$AC = \sqrt{65} \text{ units}$$

$(\frac{1}{2}$  marks)

$$BD = \sqrt{65} \text{ units}$$

$(\frac{1}{2}$  marks)

OR

Ans:

$$(x - 7)^2 + (y - 1)^2 = (x - 3)^2 + (y - 5)^2 \quad 1 \text{ mark}$$

$$x^2 - 14x + 49 + y^2 - 2y + 1 = x^2 - 6x + 9 + y^2 - 10y + 25 \quad 1 \text{ mark}$$

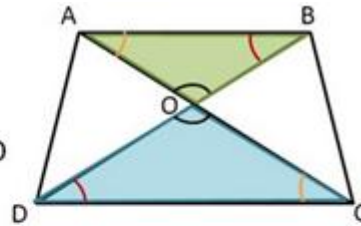
$$x - y - 2 = 0 \quad 1 \text{ mark}$$

17.

Ans:

Given: ABCD is a trapezium with  
AB || CD  
and diagonals AC & BD intersecting at O

To prove:  $\frac{OA}{OC} = \frac{OB}{OD}$



Proof: In  $\triangle OAB$  and  $\triangle OCD$

$$\angle AOB = \angle DOC \quad (\text{Vertically opposite angles}) \quad 1 \text{ mark}$$

$$\angle ABO = \angle CDO \quad (\text{since } AB \parallel CD \text{ with } BD \text{ as transversal, alternate angle are equal})$$

$$\triangle OAB \sim \triangle OCD \quad (\text{AA Similarity}) \quad 1 \text{ mark}$$

We know that if 2 triangles are similar ,  
their corresponding sides are in proportion

Hence

$$\frac{OA}{OC} = \frac{OB}{OD} \quad 1 \text{ mark}$$

Hence proved

OR

In  $\triangle ADB$

$$AB^2 = BD^2 + AD^2 \quad (\text{Pythagoras theorem})$$

$$\Rightarrow AD^2 = AB^2 - BD^2 \quad - \quad (1) \quad 1$$

Also in  $\triangle ADC$

$$AC^2 = CD^2 + AD^2 \quad (\text{Pythagoras theorem}) \quad 1$$

$$\Rightarrow AD^2 = AC^2 - CD^2 \quad - \quad (2)$$

From (1) and (2)

$$AB^2 - BD^2 = AC^2 - CD^2$$

$$\Rightarrow AB^2 + CD^2 = BD^2 + AC^2 \quad 1$$

18.

Ans:

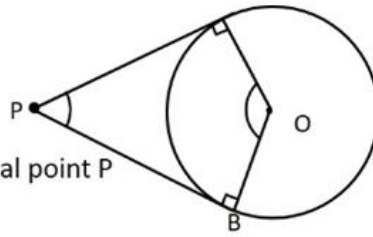
Given:

A circle with center O.

Tangents PA and PB drawn from external point P

To prove:  $\angle APB + \angle AOB = 180^\circ$

Proof:



1/2 mark

Since PA is tangent,

$OA \perp PA$

Since PB is tangent,

$OB \perp PB$

$\therefore \angle OAP = 90^\circ \quad \therefore \angle OBP = 90^\circ$       1 mark

*(Tangent at any point of circle is perpendicular to the radius through point of contact)*

In quadrilateral OAPB

$\angle OAP + \angle APB + \angle OBP + \angle AOB = 360^\circ$       *(Angle sum property of quadrilateral)*

*Putting values of angles*

1 mark

$90^\circ + \angle APB + 90^\circ + \angle AOB = 360^\circ$

$180^\circ + \angle APB + \angle AOB = 360^\circ$

$\angle APB + \angle AOB = 360^\circ - 180^\circ$

$\angle APB + \angle AOB = 180^\circ$

1/2 mark

Hence proved

19. Ans:

$$\text{LHS } \frac{\frac{\sin A}{\cos A}}{1 - \frac{\cos A}{\sin A}} + \frac{\frac{\cos A}{\sin A}}{1 - \frac{\sin A}{\cos A}} \quad 1/2 \text{ mark}$$

$$\frac{\frac{\sin A \times \sin A}{\cos A (\sin A - \cos A)} + \frac{\cos A \times \cos A}{\sin A (\cos A - \sin A)}}{\frac{\sin^2 A}{\cos A (\sin A - \cos A)} - \frac{\cos^2 A}{\sin A (\sin A - \cos A)}} \quad 1 \text{ mark}$$

$$\frac{\frac{\sin^3 A - \cos^3 A}{\sin A \cos A (\sin A - \cos A)}}{\frac{(\cancel{\sin A} \cos A) (\sin^2 A + \cos^2 A + \cancel{\cos A} \sin A)}{\sin A \cos A (\cancel{\sin A} \cos A)}} \quad 1 \text{ mark}$$

$$\frac{1 + \cos A \sin A}{\sin A \cos A} = \frac{1}{\sin A \cos A} + 1 \quad 1/2 \text{ mark}$$

$$= \sec A \operatorname{cosec} A + 1 - \text{RHS}$$

OR

Evaluate :

$$\sec^2 10^\circ - \cot^2 80^\circ - \frac{\sin 15^\circ \cos 75^\circ + \cos 15^\circ \sin 75^\circ}{\cos \theta \sin(90^\circ - \theta) + \sin \theta \cos(90^\circ - \theta)} - \tan 10^\circ \tan 20^\circ \tan 30^\circ \tan 70^\circ \tan 80^\circ$$

Ans:

$$\sec(10^\circ) = \operatorname{cosec} 80^\circ, \sin(15^\circ) = \cos 75^\circ$$

$$\operatorname{cosec}^2 \theta = 1 + \cot^2 \theta, \cot(90^\circ - \theta) = \tan \theta$$

$$\sec^2 10^\circ - \cot^2 80^\circ - \frac{\sin 15^\circ \sin 15^\circ + \cos 15^\circ \cos 15^\circ}{\cos^2 \theta + \sin^2 \theta} - \tan 10^\circ \tan 20^\circ \times \frac{1}{\sqrt{3}} \times \cot 20^\circ \cot \quad 1$$

$10^\circ$

$$\operatorname{cosec}^2 80^\circ - \cot^2 80^\circ - 1 - \frac{1}{\sqrt{3}}$$

$$1 - 1 - \frac{1}{\sqrt{3}} = -\frac{1}{\sqrt{3}} \quad 1$$

20.

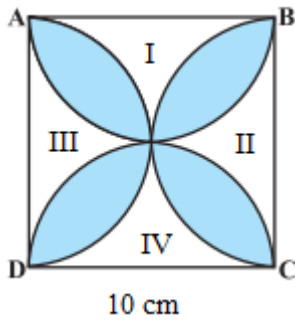
Ans:

$$2(\text{sector area} - \text{triangle area}) \quad 1 \text{ mark}$$

$$2\left(\frac{1}{4} \times \frac{22}{7} \times 8^2 - \frac{1}{2} \times 8 \times 8\right) \quad 1 \text{ mark}$$

$$\frac{256}{7} \text{ sq. cm} \quad 1 \text{ mark}$$

OR



Let us mark the four unshaded regions as I, II, III and IV (see Fig.).

Area of I + Area of III

= Area of ABCD – Areas of two semicircles of each of radius 5 cm      1/2 mark

$$= \left( 10 \times 10 - 2 \times \frac{1}{2} \times \pi \times 5^2 \right) \text{cm}^2 = (100 - 3.14 \times 25) \text{cm}^2$$

$$= (100 - 78.5) \text{cm}^2 = 21.5 \text{cm}^2 \quad \text{1 mark}$$

Similarly, Area of II + Area of IV = 21.5 cm<sup>2</sup>      1/2 mark

So, area of the shaded design = Area of ABCD – Area of (I + II + III + IV)

$$= (100 - 2 \times 21.5) \text{cm}^2 = (100 - 43) \text{cm}^2 = 57 \text{cm}^2 \quad \text{1 mark}$$

21.

Let R be the radius, and h be the height of the cylindrical portion.

Height of the building, R+h = 2R = D = internal diameter.

This gives, h = R.

1/2 mark

Volume = Volume of cylindrical portion + Volume of hemispherical portion

1/2 mark

$$= \pi R^2 h + (4\pi R^3/3)/2 = 880/21$$

$$(22/7)(R^2 h + 2R^3/3) = 880/21$$

$$R^2(h+2R/3) = 440/3$$

$$R^2(R+2R/3) = 440/3$$

$$R^3(5/3) = 440/3$$

$$R^3 = 88$$

1 mark

$$R = 4.45 \text{ m}$$

1/2 mark

and Total Height of the building, = R+h = 2R = 8.9 m

1/2 mark

22.

Ans :

Correct table

( 1 mark)

Correct graph

(1 mark)

Median = 138

( 1 mark)

### SECTION -D

23. Ans:

The time taken to fill a cistern by smaller pipe =  $x$  minutes

Work done by smaller pipe in 1 minute =  $\frac{1}{x}$

The time taken to fill a cistern by larger pipe =  $x-3$  minutes

Work done by larger pipe in 1 minute =  $\frac{1}{x-3}$

The total time taken by both the pipes together to fill the cistern =  $3\frac{1}{13} = \frac{40}{13}$  minutes

Work done by both in 1 minute =  $\frac{13}{40}$

According to the problem,

$$\frac{1}{x} + \frac{1}{x-3} = \frac{13}{40}$$

1 mark

$$13x^2 - 119x + 120 = 0$$

$\frac{1}{2}$  mark

$$b^2 - 4ac = 7921$$

$$\sqrt{7921} = 89$$

$$x = \frac{-(-119) \pm 89}{26} = 8 \text{ or } \frac{30}{26}$$

1 mark

Rejecting  $x = \frac{30}{26}$  (since less than 3)

$\frac{1}{2}$  mark

Hence, the larger pipe takes  $8 - 3 = 5$  minutes

smaller pipe takes  $x = 8$  minutes

(1 mark)

**OR**

Ans:

Let the speed of the stream be  $x$  km/hr

$$\frac{12}{11-x} + \frac{12}{11+x} = \frac{11}{4}$$

1 mark

$$x^2 - 121 + 96 = 0$$

$1\frac{1}{2}$  marks

$$x \neq -5, x = 5$$

1 mark

speed of stream = 5 km/h

$\frac{1}{2}$  mark

24. Ans:

(a) Number of trees planted by class I = 3

Number of trees planted by class II =  $3 \times 2 = 6$

Number of trees planted by class III =  $3 \times 3 = 9$

...

Number of trees planted by class XII =  $12 \times 3 = 36$

(2 marks)

The number of trees form an A.P



i.e 3,6,9,12,... , 36 ,  $n = 12$

$$S_n = \frac{12}{2} (3 + 36) = 234 \quad (1 \text{ mark})$$

Hence the total number of trees that will be planted by the students is 234.

(b) Yes. Planting more trees helps in reducing pollution and thus, make environment clean and green. (1 mark)

25.

Ans:

Given, To prove, Diagram, Construction

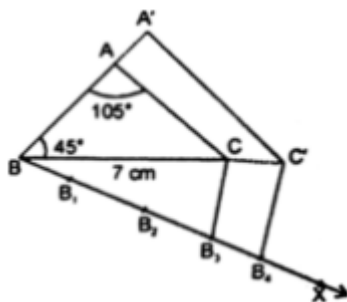
1 mark

Correct Proof

3 marks

26.

Ans:



Construction of triangle ABC

1 mark

Construction of similar triangle

3 marks

27.

$$\text{LHS } \frac{\frac{\sin A}{\cos A}}{1 - \frac{\cos A}{\sin A}} + \frac{\frac{\cos A}{\sin A}}{1 - \frac{\sin A}{\cos A}}$$

$$\frac{\sin A \times \sin A}{\cos A (\sin A - \cos A)} + \frac{\cos A \times \cos A}{\sin A (\cos A - \sin A)}$$

1 mark

$$\frac{\sin^2 A}{\cos A (\sin A - \cos A)} - \frac{\cos^2 A}{\sin A (\sin A - \cos A)}$$

$$\frac{\sin^3 A - \cos^3 A}{\sin A \cos A (\sin A - \cos A)}$$

1 mark

$$\frac{(\cancel{\sin A} - \cancel{\cos A}) (\sin^2 A + \cos^2 A + \cancel{\cos A} \cancel{\sin A})}{\sin A \cos A (\cancel{\sin A} - \cancel{\cos A})}$$

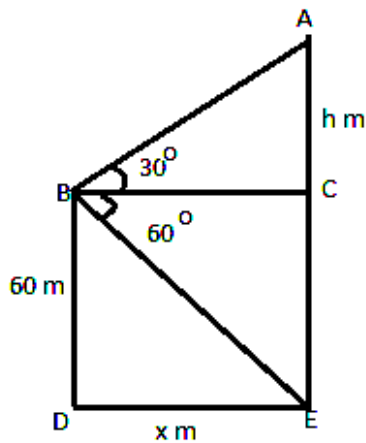
1 mark

$$\frac{1 + \cancel{\cos A} \cancel{\sin A}}{\sin A \cos A} = \frac{1}{\sin A \cos A} + 1$$

$$= \sec A \operatorname{cosec} A + 1 = \text{RHS}$$

1 mark

28.



Let  $BD = 60$  m be the height of the building.

Let A and E be the top and bottom position of the light house.

Let  $h$  be the difference of heights of the building and the light house.

Let  $x$  be the distance between light house and the building.

Consider the triangle ABC

In  $\triangle ABC$ ,  $BC = \sqrt{3}h$  ( 1 Mark)

In  $\triangle BCRE$ ,  $BC = \frac{60}{\sqrt{3}}$  ( 1 Mark)

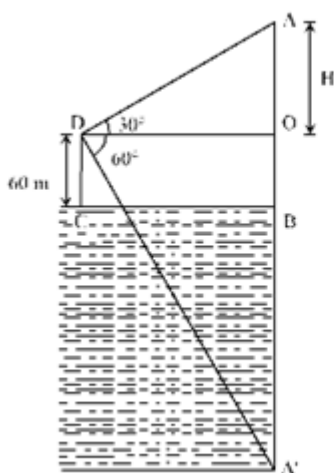
$h = 20$  m ( 1 Mark)

$BC = 20\sqrt{3}$  m ( $\frac{1}{2}$  Marks)

Difference between the height = 20 m

distance between them =  $20\sqrt{3}$   $\frac{1}{2}$  marks

**OR**



Let  $AO = H$

$CD = OB = 60$  m

$A'B = AB = 60 + H$

In  $\triangle AOD$ ,

$$\tan 30^\circ = \frac{AO}{OD} = \frac{H}{OD}$$

$$H = \frac{OD}{\sqrt{3}}$$

$$OD = \sqrt{3}H$$

1 mark

Now, In  $\triangle A'OD$ ,

$$\tan 60^\circ = \frac{OA'}{OD} = \frac{OB + BA'}{OD}$$

$$\sqrt{3} = \frac{60+60+H}{\sqrt{3}H} = \frac{120+H}{\sqrt{3}H} \quad 1 \text{ mark}$$

$$\Rightarrow 120 + H = 3H$$

$$\Rightarrow 2H = 120$$

$$\Rightarrow H = 60 \text{ m}$$

1 mark

Thus, height of the cloud from the surface of the lake = AB + A'B = 60 + 60 = 120 m. 1 mark

29. Ans:

$$l = 31.62 \text{ cm} \quad 1 \text{ mark}$$

$$\text{S.A} = 3295.6 \text{ cm}^2 \quad 1 \text{ mark}$$

$$\text{Volume} = 22000 \text{ cm}^3 \quad 1 \text{ mark}$$

$$\text{Cost of milk} = \text{Rs: } 550 \quad 1 \text{ mark}$$

30.

Marks	Frequency	$x_i$	$u_i = \frac{x_i - 67.5}{5}$	$f_i u_i$
50-55	5	52.5	-3	-15
55-60	8	57.5	-2	-16
60-65	15	62.5	-1	-15
65-70	11	67.5	0	0
70-75	7	72.5	1	7
75-80	4	77.5	2	8
	50			-31

( 2 Marks)

$$\bar{u} = \frac{-31}{50}$$

$$\bar{x} = a + h\bar{u} = 64.4 \quad ( 2 \text{ Marks})$$

OR

$x_i$	Number of Workers	$u_i = \frac{x_i - 45}{10}$	$f_i u_i$
5	5	-4	-20
15	7	-3	-21
25	$f_1$	-2	$-2f_1$
35	3	-1	-3
45	$f_2$	<b>0</b>	<b>0</b>
55	9	1	9
65	6	2	12
<i>Total</i>	$30 + f_1 + f_2$		$-23 - 2f_1$

(1 Mark)

$$f_1 + f_2 = 70$$

(1 mark)

$$f_1 = 20$$

(1 mark)

$$f_2 = 50$$

(1 mark)